Does the ECB Rely on a Taylor Rule?
Comparing Ex-post with Real Time Data

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Does the ECB Rely on a Taylor Rule?
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by

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Abstract

We assess the differences that emerge in Taylor rule estimations for the ECB when using ex-post data instead of real time forecasts and vice versa. We argue that previous comparative studies in this field mixed up two separate effects. First, the differences resulting from the use of ex-post and real time data per se and, second, the differences emerging from the use of non-modified real time data instead of real-time data based forecasted values and vice versa. Since both effects can influence the reaction to inflation and the output gap either way, we use a more clear-cut approach to disentangle the partial effects. Our estimation results indicate that using real time instead of ex post data leads to higher estimated inflation coefficients while the opposite is true for the output gap coefficients. If real time data forecasts for the current period are used (since actual data become available with a lag), this empirical pattern is even strengthened in the sense of even increasing the inflation response but lowering the reaction to the output gap while the reverse is true if “true” forecasts of real time data for several periods are employed.

JEL codes: E43, E58

Keywords: European Central Bank, monetary policy, real time data, Taylor rule

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1. Introduction

Ever since the founding of the European Central Bank (ECB) in 1999 the question was raised whether it follows or should follow the by now famous Taylor rule (Taylor (1993)). In fact many economists so far have investigated this issue with respect to the euro area using either data of a “fictitious” ECB prior to its establishment (see e.g. Peersman and Smets (1999), Gerlach and Schnabel (2000), Clausen and Hayo (2002), Altavilla and Landolfo (2005)) or the limited data thereafter (see e.g. Surico (2003), Fourçans and Vranceanu (2003), Gerdesmeier and Roffia (2003), Garcia-Iglesias (2007), Belke and Polleit (2007) and Fendel and Frenkel (2009)).\footnote{In fact, also combinations of these two types can be found, mostly to expand the sample in order to generate more reliable estimates (see e.g. Gerlach-Kirsten (2003), Siklos and Bohl (2009)). For a comparison between these two types of data at the early stage see Ullrich (2003).} By now we have seen more than ten years of ECB monetary policy and are now able to derive new estimates from a sufficiently broad euro area-specific database even if quarterly data are used.

But the whole array of Taylor rule estimations enumerated above essentially rely on ex-post data. This comes as a surprise as the use of ex-post data “is based on unrealistic assumptions about the timeliness of data availability and ignores difficulties associated with the accuracy of initial data and subsequent revisions” (Orphanides (2001), p. 964). Therefore, the analysis should be carried out using real time data instead of ex-post data simply because the latter were not available to the central bank decision making body at the time the interest rate decision was made. That is exactly why we focus on the extent of quantitative differences between the estimates occurring from using ex-post instead of real time data.
To be more specific, these quantitative differences potentially stem from four sources. First, inflation and output gap data are available only with a lag. Second, data sets are revised as time goes by (‘data uncertainty’). Third, the central bank governing council can construct the variables needed based only on past data and not with reference to the whole relevant sample period as is the case with ex-post data, since when the council constructs these variables it cannot “look back” at the whole sample (‘statistical uncertainty’), and, fourth (and less specific for the problem investigated here), the empirical model used to derive the estimates is not unique (‘model uncertainty’).

However, in our paper we do not only focus on the changes in numerical values of estimation results arising from the use of ex-post instead of real time data but also on those stemming from the use of forecasted variables instead of contemporaneous ones since central banks would react systematically too late when applying only contemporaneous variables because monetary impulses become effective with a lag (see, for instance, Svensson (2003), p. 449). In principle, there are two ways in which this comparison can be enacted: either by using ex-post data or by applying real time data. However, we prefer to follow the latter approach because it appears to us more realistic that the ECB builds its forecast upon real time data than on the (not available) ex-post data. Another advantage of this approach is that we are able to use a transparent procedure by comparing estimates based on ex-post with those employing real time data and, later on, comparing real time data estimates with estimates based on variable forecasts based on real time data.

So far, estimations of ECB Taylor rules using real time data are still quite scarce. Any attempts to conduct a similar approach as we do in this paper did not lead to overall conclusive results so far. In fact, there is only a couple of papers
available dealing with this topic. Due to data limitations, they all focus exclusively on monthly data or mainly even only on the pre-ECB era. Therefore, we present estimates based on monthly and quarterly data which rely exclusively on the EMU sample period.

The paper proceeds as follows. In section 2, the Taylor rule and its extensions are described before we turn to the pattern of results gained in this field so far in section 3. In section 4, we explain our data choice and variable selection. In section 5 we display our estimation results. Section 6 finally concludes.

2. The Taylor rule

It is well over a decade since John B. Taylor set out what has become part of the current orthodoxy of monetary economics by now. In 1993 he proposed a new and simple monetary policy rule which suggests that the central bank should set interest rates according to deviations of the inflation rate from its target and the percentage deviations of the output from its potential (the so called output gap). So the rule can be derived in the following way:

\[ i_t = r_t^* + \pi_t + \alpha_\pi (\pi_t - \pi^*) + a_y (y_t - y_t^*), \]

where \( i_t \) is the interest rate set by the central bank, \( r_t^* \) stands for the equilibrium real interest rate, \( \pi_t \) is the inflation rate over the previous four quarters, \( \pi^* \) represents the constant inflation target, \( (y_t - y_t^*) \) stands for the output gap and \( \alpha_\pi, a_y \) are coefficients measuring the strength of the reaction to the inflation and output gap. Both coefficients are expected to be larger than zero. In fact, Taylor (1993) himself proposed that each coefficient should be equal to 0.5.\(^2\) All variables

\(^2\) However, Ball (1999) argues that the coefficients need to be adjusted in order to display an optimal policy reaction. Accordingly, also Belke and Polleit (2009), pp. 714ff. and 765ff., conclude that
with the exception of the inflation target are allowed to vary over time and are therefore indexed by $t$. However, in the literature this is the exception rather than the rule with respect to $r_t^*$ when it comes to Taylor rule estimations. For this purpose, we use the Fisher equation with adaptive expectations ($r_t = i_t - \pi_t$) and apply the Hodrick-Prescott filter (HP-Filter) (see Hodrick and Prescott (1997)) to the resulting real interest rate variable. In order to construct our variable measuring potential output $y_t^*$, we also apply the HP-Filter. However, we check for the robustness of our estimation results by constructing this variable with the help of a linear and a quadratic trend because mis-measurement of the potential output has the potential to cause serious problems in Taylor rule estimations especially when the underlying output time series is based on real time data.\footnote{The choice of the correct potential output measure is of course one possible source of measurement problems of the Taylor rule.} 

For estimation purposes equation (1) can be rearranged as follows:

\begin{equation}
(2) \quad i_t = r_t^* - (a_\pi - 1) * \pi^* + a_\pi (\pi_t) + a_y (y_t - y_t^*),
\end{equation}

with $a_\pi = 1 + \alpha_\pi$. In the notation of equation (2), the Taylor principle implies that the coefficient $a_\pi$ needs to be larger than unity in order to raise the nominal interest rate by more than the inflation rate and, by this, to lower the real interest rate which is the decisive variable for investment or consumption decisions. If $a_\pi < 1$, the real interest rate would decrease if inflation is rising, leading to even more inflationary pressure in the future. Since Taylor proposed $\alpha_\pi = 0.5$ it immediately follows that $a_\pi = 1.5$. 

\footnote{See Orphanides and van Norden (2002) for a detailed discussion on the unreliability of output gap estimates in real time. See Gros, Mayer and Ubide (2005), p. 10, for the same discussion in the context of EMU as a special case.}
The first commonly used extension of the Taylor rule is the inclusion of an interest rate smoothing term to account for the fact that central banks typically adjust the key interest rate in rather small steps without hardly ever revising the direction thereafter. In this case, equation (2) turns into:

\[ i_t = \rho * i_{t-1} + (1 - \rho) * \left[ r^*_t - (a_\pi - 1) * \pi^* + a_\pi (\pi_t) + a_y (y_t - y^*_t) \right], \]  

where \( \rho \) represents the smoothing parameter. If \( \rho = 1 \) the interest rate is solely influenced by the past interest rate and for \( \rho = 0 \) equation (2) reduces to equation (1). However, as experience shows, reasonable results should lie somewhere in between \( 0 < \rho < 1 \).

A second extension is the forward-looking perspective. Clarida and Gertler (1996), for instance, argued in favor of using a forward-looking specification of the Taylor rule because any other specifications would imply that the central bank would respond systematically too late as monetary impulses become effective only with a lag. Therefore, they proposed to use expected future values of the inflation rate based on the information available at the point in time where the decision is made. Later on this concept was expanded to the use of forecasts for the output gap as well. So a forward-looking Taylor reaction function would look like this:

\[ i_t = \tilde{r}^*_t - (a_\pi - 1) * \pi^* + a_\pi * E (\pi_{(t+j|t)}) + a_y * \left[ E (y_{(t+k|t)}) - \bar{y}^*_t \right], \]

where \( E \) is the expectations operator and \( j,k \) are some positive values indicating the forecast horizon. Note that \( j \) and \( k \) need not be equal so that different forecasts horizons for the inflation rate and the output are possible. With forecasts used in the Taylor rule also the variables \( \tilde{r}^*_t \) and \( \bar{y}^*_t \) are adjusted because in the former case the expected inflation measure alters and in the latter case the trend changes because of more data.
It is of course possible to complement forward-looking Taylor rules with an interest rate smoothing term and this is in fact done in most of the cases. However, imposing forward-looking elements onto the Taylor reaction function only makes sense in the context of real time data because these were the data the central bank has based its forecasts on. In contrast, extracting forecasts from ex-post data means forming forward-looking expectations based on data which were de facto not available at the time of decision making which is quite unrealistic.

Therefore, the approach carried out here is a three-step one. First, we estimate Taylor reaction functions with ex-post data. Second, we compare the resulting estimates with those gained for estimates of the Taylor rule based on unmodified pure real time (which are available to the decision making body “contemporarily”) data. Third, we assess the differences between real time data based estimated Taylor rules and the ones which rely on forecasted variables based on real time data.

3. Survey of the literature

As mentioned above, up to now the available empirical work providing Taylor rule estimates in real time for the euro area is by far not exhaustive. Nevertheless, their findings are worth mentioning here because they are natural candidates for comparisons to the results derived from the analysis carried out in our paper. We pick up five of them in the following.

In Adema (2004), Taylor rule estimates using ex-post and “quasi” real time data are compared. The difference between real time and “quasi” real time data is simply that data revisions are supposed to be fairly small and can thus be neglected. Making this assumption, Adema ends up with coefficients $\rho = 0.75$, $\alpha_r = 1.80$, $\alpha_v =$
\(a_y = 1.72\) for ex-post and \(\rho = 0.64\), \(\alpha_\pi = 1.89\), \(a_y = 0.46\) for “quasi” real time data covering the sample period 1994Q1 to 2000Q4 thus mostly the pre-ECB era.

In the same vein as Adema is the paper by Carstensen and Colavecchio (2004). The authors limit themselves to an estimation of Taylor rules with “quasi” real time data but do not compare their results to Taylor rules using ex-post estimates. Thus, they do not only neglect the data revisions but also abstract from any time lag problem. This is exactly why their results are, in the quantitative dimension, somewhere in between Taylor rules estimated with ex-post and those based on real time data. For the sample period 1999M1 – 2004M2 they come up with coefficients \(\rho = 0.95\), \(\alpha_\pi = 1.01\) and \(a_y = 1.36\).

Gerdesmeier and Roffia (2004) are among the first authors using real time data instead of quasi real time data. They estimate Taylor rule coefficients for the period 1999M1 – 2003M6. For ex-post data they find \(\rho = 0.84\), \(\alpha_\pi = 1.08\), and \(a_y = 0.70\). When using contemporaneous realizations of real time data, the picture changes as in this case the estimated output gap coefficient increases (2.05) while the estimated inflation parameter falls far below unity (0.39). The degree of interest rate smoothing decreases to 0.63. However, conducting their analysis with twelve month forecasts of the independent macro variables based on survey data collected in real time, they arrive at much higher values for the estimated coefficient of inflation (1.31) while \(\rho\) and \(a_y\) remain more or less unchanged (\(\rho = 0.71\) and \(a_y = 1.95\)). The already rather high estimated inflation coefficient gets even larger when applying a two year instead of a one year forecast based on real time survey data (\(\alpha_\pi = 2.91\), \(\rho = 0.67\), and \(a_y = 2.02\)).

Working with ex-post data, Sauer and Sturm (2007) find coefficients of \(\rho = 0.94\), \(\alpha_\pi = -0.84\), \(a_y = 1.45\) for the period ranging from January 1999 to
October 2003. Employing real time data instead, the estimated coefficients turn out to be $\rho = 0.98$, $a_\pi = -0.27$ and $a_y = 3.01$ result. When they implement forecasts of the independent macro variables based on real time data, the estimated inflation coefficient becomes positive and larger than unity (6.62) and the estimated interest rate smoothing parameter and the estimated coefficient of the output gap become $\rho = 0.98$ and $a_y = 9.24$, respectively. However, in all cases the Taylor rule coefficients are insignificant which is probably due to the large estimated interest smoothing parameter.

Finally, Gorter, Jacobs and De Haan (2008) compare estimates of the ECB Taylor rule using ex-post data with estimates based on independent macro variables which are forecasted based on real time data.\(^5\) For the period 1997M1 – 2006M12, they find estimated coefficients for the former equal to $\rho = 0.95$, $a_\pi = 0.09$ and $a_y = 0.37$ and $\rho = 0.86$, $a_\pi = 1.39$, $a_y = 1.52$ for the latter. However, we would like to argue that their approach is unable to distinguish between the effects of using real time instead of ex-post data and the one induced by the use of forecasts.

4. The data issue

To our knowledge, so far only Adema (2004) has estimated Taylor rules using (quasi) real time and quarterly data but this mainly for the pre-ECB era. Our Taylor rule estimations for the EMU period are based on quarterly and monthly data. Hence, a side-effect is that in our paper we are able to check whether the estimation results closely correspond with other (as is fortunately corroborated later on by our analysis). All data are taken from the Euro Area Business Cycle Network (EABCN) real time database. The output variable is captured as usual by real GDP (for

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\(^5\) This study relies on survey data of real time forecasts made by major banks in the EMU.
quarterly data) and industrial production (for monthly data). The price level is proxied by the harmonized index of consumer prices (HICP) and the interest rate variable by the three-month Euribor. Unfortunately, these data are only available from 2001 onwards so that the data before (1999 and 2000) have been collected from the ECB monthly bulletins.

All data are seasonally adjusted and cover the euro area consisting of its first twelve members for the sample period 1999Q1 (1999M1) to 2007Q2 (2007M6). We choose the specific end of the sample period with an eye on the fact that the data provided by the EABCN are cut off in March 2008. To account for ex post data adjustments even at the end of the sample period which have the potential to lead to differences of estimation results, dependent on the use of ex-post versus real time data, we decided to leave ample room of three quarters for revisions. With this, we are in line with the findings and recommendations by Coenen, Levin and Wieland (2005). Hence, in our case the ex-post variables are those available in 2008M3 for the whole estimation period (1999M1 to 2007M6). In the case of the interest rate this is also the (forecasted) real time series because the interest rate is not subject to the real time critique. In contrast to that, the other real time data are known by the ECB governing council at the time the decision was made and, hence, represent exactly the information that could explain interest rate rises/ cuts. Unfortunately, the last values known to the ECB are never the contemporaneous ones as information about them becomes available only with a lag. Therefore, when using real time data, the ECB would react systematically too late in the sense that it reacts to values which are not up to date.

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6 Thus, we include Greece which joined the EMU in 2001 and omit Slovenia which became a member not earlier than 2007.
That is why forecasts of the variables included in the Taylor reaction function need to be implemented. It appears straightforward to construct forecasts covering exactly that “time lag deficit” because in this case a comparison between ex-post and real time data would rely exactly on the same time periods. So this type of forecast is applied by us as a first strategy.

But as the ECB monetary strategy is medium term oriented it also appears reasonable to incorporate a really forward-looking forecast. We use this as our second empirical strategy. Here, we strictly follow Sauer and Sturm (2007) who implement forecasts of 6 months for inflation and 3 months for the output gap. Using these forecast horizons, we address the ECB’s medium term orientation. What is more, we take into account that the primary goal of the ECB is to maintain price stability since the smaller forecast horizon of the output gap takes the future inflationary pressures associated with this variable into account.

A second problem which emerges along with forecasts is the choice of the forecasting method to mimic forward-looking behavior of the monetary authority since there are no reliable ECB internal data available to the researcher. So the resulting Taylor rule estimates using calculated forecasts or survey data are just as good to the extent to which they coincide with the ECB forecasts. So what forecast technique is the most preferable in our context? In the absence of reliable forecast databases, we decided to strictly follow Sauer and Sturm (2007) by employing an AR(3) process to model monthly forecasts. For the purpose of quarterly forecasting we decided to use an AR(2) process.

Obviously, the respective forecasts have to be as close as possible to the (unknown) ECB predictions to be good forecasts in the sense of modeling the Taylor rule correctly and not close to the true values emerging several periods thereafter. If the ECB does not make any forecast errors at all (perfect foresight) then the ECB forecasts and “true” values would be the same. However, this is quite unrealistic.

We also experimented with different AR processes but the results did not change significantly. The results are available on request.
Coming back to the Taylor rule, there are in fact five variables that are needed. First, the interest rate \((i_t)\), second, the equilibrium real interest rate \((r^*_t)\), third, the inflation target \((\pi^*)\), fourth, the inflation rate \((\pi_t)\) and fifth, the output gap \((y_t - y^*_t)\) which consists of an output measure and the potential output.

Turning from the least to the most complex variable, we start with the inflation target which is simply set equal to two percent in line with the ECB announcement to define price stability with a increase of HICP of close to but less than two percent over the medium term. The interest rate can be taken directly from the database without any adjustment. As a measure of the inflation rate, the year-on-year increase in the HICP is taken. Hence, the formula constructing the inflation rate looks like this:

\[
\pi_t = 100 \times \left[ \log(HICP_t) - \log(HICP_{t-12}) \right] \quad \text{(for monthly data)}
\]

\[
\pi_t = 100 \times \left[ \log(HICP_t) - \log(HICP_{t-4}) \right] \quad \text{(for quarterly data)}
\]

Applying these transformations to ex-post data is a trivial task but when it comes to real time data it gets slightly more complicated because in every period the last available value has to be diminished by its value one year ago. However, due to the existence of the time lag, the last value available is never the actual value. For monthly data, the lag is normally two months and for quarterly data one quarter.

To construct the output gap variable, a measure of the potential output is needed. In the literature the HP-Filter is commonly used. However, the HP-Filter is as a de-trending method not necessarily displaying the correct path of the output potential.\(^9\) Therefore, we also use potential output measures based on a linear and,  

\(^9\) See for an extensive comparison between various types of potential output gap measures and their relevance for output gap estimates Chagny and Döpke (2001).
alternatively, a quadratic trend. When the HP-Filter is employed the smoothing parameter is set to 14.400 for monthly and 1.600 for quarterly data. With these potential output measures it becomes possible to calculate the output gap which is done using the following transformation:

\[
Y_t = 100 \times [\log(y_t) - \log(y_t^*])
\]

In case of ex-post data it is again straightforward to calculate the output gap because here the potential output can be built over the whole sample period. To get the output gap in real time is, however, much harder because initially after the start of EMU there were only data of the pre-ECB era available to construct the potential output. The question is now how far this data set needs to reach into the past to generate reliable estimates of the potential. In the following, we use the data of the ten preceding years, thus, the output gap in 1999M1 was built on the data going back to 1989M1. However, it is clearly at odds with the experience of any observer that the ECB is deriving its potential output estimates still today from data of 1989. So every real time estimate relies on the preceding ten years of data. For instance, in order to construct the output gap in real time for every month/quarter, the output gap is calculated with the data of the preceding ten years and the last value of this 10-year period is taken as the data point of the respective period in real time. As an example, in 1999M1 the output gap is estimated based on the data ranging from 1989M1 to 1999M1 and value of the time series in the last month is taken as the data point of the output gap for 1999M1 in real time. We apply the same procedure for all other periods as well in order to generate the output gap in real time. In order to

\[10\] The linear de-trended potential output is generated by the expression \( y_{t,lin}^* = y_{0,lin}^* + \alpha \times t \), while the potential output computed imposing a quadratic trend is derived from the transformation \( y_{qua}^* = y_{0,qua}^* + \beta \times t^2 \), with \( \alpha \) and \( \beta \), respectively, being the slope coefficients.

\[11\] In this example, we neglect the time lag problem for reasons of simplicity but we account for it when constructing the respective time series.
account for the well-known end-of-sample bias induced by the HP-Filter, we use forecasts of the output series to expand the sample and avoid this problem.

The last independent macro variable that needs to be specified is the equilibrium real interest rate. In fact, the equilibrium real interest rate has in the context of Taylor rules almost never played the role it should have because it was mainly just held constant over time by making it a part of the constant in econometric analysis.\textsuperscript{12}

However, there is considerable uncertainty about how to calculate the non-observable equilibrium real interest rate. It may be approximated by a multi-year average of the difference between the actual nominal interest rate and inflation. However, such a measure would depend on the period used for forming the average. Alternatively, assuming a constant equilibrium real interest rate over long periods may not be appropriate either. Besides the expected rate of return on tangible fixed assets and the general propensity to save, the equilibrium real interest rate may also depend on the general assessment of the uncertainty in the economy and the degree of credibility of the central bank. If these aspects are not taken into account, the resulting Taylor rate may be of questionable informative value.

Seen on the whole, thus, it is widely agreed upon by economists that the equilibrium real interest rate is by no mean constant over time\textsuperscript{13} and should be allowed to fluctuate just like other variables. Hence, we insert an explicit measure of the equilibrium real interest rate into the Taylor rule specification by using the Fisher equation with adaptive expectations to construct the real interest rate

\begin{equation}
    r_t = i_t - \pi_t,
\end{equation}

\textsuperscript{12} A notable exception from this rule is Plantier and Scrimgeour (2002).
\textsuperscript{13} For the case of the euro area see Cuaresma, Gnan and Ritzberger-Gruenwald (2004), Mésonnier and Renne (2007), Garnier and Wilhelmson (2009).
and finally employ the HP-Filter to the resulting time series. Applying de-
trending methods is probably the easiest and less precise way to calculate the
equilibrium level but as Wu (2005) puts it: It is “reasonable over periods where
inflation and output growth are stable” which is the case for the sample period
investigated by us. This leads to the time series of the equilibrium rate as shown in
Figure 1.

1. Figure 1 about here -

In this figure, the calculated paths of the equilibrium real interest rate for monthly
and quarterly, ex-post and real time data are displayed. It is obvious that the rate is
by no means constant over time. In fact, its absolute deviation over time amounts to
about 2.5 percent. For an “equilibrium” interest rate, the gyrations appear to be rather
strong. However, the scale of our calculations is in line with the real equilibrium
interest rates calculated by other authors such as, for instance, Cuaresma, Gnan and
Garnier and Wilhelmsen (2009), p. 310, who all come up with a similar variance. A
second striking observation is that the shapes of the curves turn out to be rather
similar – independent on whether they are based on ex-post or on real time data.
Hence, differences in the Taylor rule coefficients cannot be explained by differences
in this measure.

5. Estimation results

We now estimate Taylor reaction functions using GMM. As instruments we employ
only lagged values of the right hand side variables. In the case of monthly data, our
set of instruments comprises the last six months of inflation and the output gap and
whenever implemented two to six lags of the interest rate. When we use quarterly
data, the maximum number of lags is reduced from six to four.\footnote{The choice of the instruments was made in line with the empirical literature in this field so far. For monthly data this is Sauer and Sturm (2007) and for quarterly data Belke and Polleit (2007). We also considered to use information criteria in order to extract the “best” specification but this would mean employing a different set of instruments to each estimate. As this different choice of instruments is an additional source of differences between the estimates, we decided to rely on a constant set of instruments.} Whenever it is necessary according to the usual diagnostics, up to six lags of the equilibrium real interest rate are included. As the relevant weighting matrix we choose the heteroskedasticity and autocorrelation consistent HAC matrix by Newey and West (1987).

Our regression equations are directly derived from equations (2) to (4) which were explained in section 2. For estimation purposes they can be written as follows:

\[ (2a) \quad i_t = a_0 + r_t^* - (a_\pi - 1) \ast 2 + a_\pi (\pi_t) + a_\gamma (Y_t) + \epsilon_t \]

\[ (3a) \quad i_t = \rho \ast i_{t-1} + (1 - \rho) \ast [a_0 + r_t^* - (a_\pi - 1) \ast 2 + a_\pi (\pi_t) + a_\gamma (Y_t)] + \epsilon_t \]

\[ (4a) \quad i_t = a_0 + \tilde{r}_t^* - (a_\pi - 1) \ast 2 + a_\pi \ast E(\pi_{(t+j|t)}) + a_\gamma \ast [E(y_{(t+k|t)}) - \tilde{y}_t^*] + \epsilon_t \]

Here, the constant \( a_0 \) is expected to be equal to zero because all variables typically included in the constant (namely the equilibrium real interest rate and the inflation target) in the reduced form of the Taylor reaction function are now explicitly appearing in the Taylor rule specification. In fact, we even go beyond these three specifications by adding forecasts to the interest rate-smoothed Taylor rule and, by this, in a way merging eqs. (3a) and (4a). We display first eyeball evidence of potential numerical differences in the realization of ex-post and real time data based variables in Figures 2 and 3.

\[ - \text{ Figures 2 and 3 about here } - \]

Figure 2 gives an overview of the respective inflation rates. It becomes obvious that the differences do mainly occur because of the imposed time lag of two
months and one quarter respectively (see section 4). This does not come as a surprise as inflation data are not affected by statistical uncertainty (inflation rates get calculated instead of estimated) and are typically hardly ever revised later on.

In contrast to that, the output gap time series displayed in Figure 3 differ quite considerably in many cases. Especially at the start of our sample period the empirical realizations of the output gap deviate significantly from each other, indicating large statistical uncertainty and data revisions. With the exception of the lower two graphs which cover output gaps calculated using a potential output constructed with a quadratic trend, it becomes evident that both lines move closer together after the first years. Thus, we feel legitimized to conclude that there was less statistical uncertainty and data revisions thereafter.

5.1 Estimations of original Taylor rules – ex-post versus real time data

We now make use of this array of variables to estimate the coefficients of differently specified Taylor reaction functions. Table 1 displays the respective estimations of the original Taylor rule without any interest rate-smoothing and any forward looking components.

- Table 1 about here -

Looking at the results displayed in Table 1, the first stylized fact is that ex-post and in real time the coefficients of the inflation rate and the output gap are almost always significantly different from zero while this is hardly ever the case for the constant term \( a_0 \). This clear empirical pattern provides evidence in favor of the hypothesis that the inflation target and the equilibrium real interest rate are indeed
the only terms influencing the constant and by modeling them explicitly, the constant becomes zero.

If we base our estimations on ex-post data (columns 1.1 to 1.6), the Taylor principle \( (a_\pi > 1) \) is always violated. According to this interpretation, the ECB has followed a destabilizing policy, thus accommodating inflationary or deflationary deviations from the macroeconomic equilibrium in the economy. However, this picture clearly flips to the better side when we use real time data (columns 1.7 to 1.12). In this case, the \( a_\pi > 1 \) condition is fulfilled throughout our estimations with the only exception of column 1.7. What is more, the estimated coefficients in fact approach the value of 1.5 as proposed by Taylor. Hence, in real time the ECB has clearly followed a policy of fighting inflation quite aggressively.

However, regarding the output gap coefficient the opposite holds true. Here, the reaction is larger if we use ex-post data (columns 1.1 to 1.6), thus indicating a more active response to this variable. In contrast to that, the output gap variable seems to be less important in real time (columns 1.7 to 1.12) even though it remains significant with the expected positive sign.

These findings contradict those gained by Gerdesmeier and Roffia (2004) who estimate a stronger reaction of the ECB to the output gap in real time compared to the ex-post data scenario while inflation gets less important. Both the longer sample period we have used\(^{15}\) and the different choice of instruments we have preferred might be possible explanations for these different results. However, our results closely correspond with those found by Sauer and Sturm (2007) for the Taylor rules without interest rate smoothing even though their inflation coefficient estimated in real time does not exceed unity.

\(^{15}\) Our estimates cover the period up to mid-2007, thus they cover almost four years more than the study by Gerdesmeier and Roffia (2004).
But not only the choice of ex-post versus real time data but also the use of quarterly (columns 1.4 to 1.6 and 1.10 to 1.12) versus monthly data (columns 1.1 to 1.3 and 1.7 to 1.9) makes up for significant differences in the estimation results. Independent of the use of ex-post or real time data, the coefficients derived from quarterly data are always larger than those stemming from estimations based on monthly data. This implies that the ECB reacts more aggressively to the inflation rate and the output gap at a quarterly frequency than on a monthly basis.

5.2 Estimations of Taylor rules with interest rate smoothing – ex-post versus real time data

Summarizing, for the Taylor rule without interest rate smoothing the differences of results are quite substantial. Whether this remains true for Taylor rules including interest smoothing can be judged based on the entries in Table 2.

- Table 2 about here -

The inclusion of the interest rate smoothing term changes the results quite considerably. In case of monthly data (columns 2.1-2.3 and 2.7-2.9), the lagged interest rate always comes out to be highly significant and amounts to values of above 0.7 in all specifications. If quarterly data are used (columns 2.4-2.6 and 2.10-2.12), the degree of interest rate smoothing is less clear since its variance is higher: the empirical realization of the estimated $\rho$ ranges from 0.43 to 0.95.

However, at least for monthly data a clear empirical pattern emerges from Table 2. If we use ex-post data (columns 2.1-2.3), the interest smoothing parameter, although still relatively high, turns out to be always lower than in the real time data case (columns 2.7 -2.9) where the coefficient is close to unity in all specifications.
For quarterly estimates such a conclusion is only valid for cases in which we use the HP-filtered output gap (column 2.10). This finding is in line with the recommendation raised by Orphanides (2003) that central bankers should avoid over-reactions, given that the available real time data may be subject to substantial mis-measurement.

Unfortunately, the Taylor rule coefficients get estimated very poorly in the case of real time data. This might be mainly due to the high empirical realizations of the smoothing parameter. In fact, there are only three out of six specifications where the Taylor rule coefficients are significantly different from zero (columns 2.8, 2.11 and 2.12). Here, the Taylor principle is again fulfilled but now also a larger estimated coefficient emerges for the output gap compared to the findings in Table 1. However, in the three other cases (columns 2.7, 2.9 and 2.10) in which the Taylor rule coefficients are insignificant the present realization of the interest rate is the best predictor of the future, i.e. one period-ahead, interest rate.

Overall, it turns out that the Taylor rule coefficients are estimated more precisely with *ex-post data*. In fact, with only one exception (column 2.6) the estimated coefficients are highly significant. In contrast to the estimates conducted using ex-post data without a smoothing parameter (columns 1.1 to 1.6), the coefficient of inflation now satisfies the Taylor principle in the majority of the cases. What is more, the output gap coefficient tends to increase slightly.

A systematic comparison of the performance of the Taylor rule estimations in the “ex-post data” and “real time data” scenarios does only make sense, if we arrive at significant estimates for both types of data. A closer look at Table 2 reveals that this is only the case for linear trend estimates (columns 2.2 and 2.5 for ex-post data, 2.8 and 2.11 for real time data, respectively). The coefficient of inflation increases, if
we employ real time data like it was the case in Table 1. However, for the output gap a slightly more ambiguous pattern emerges since its estimated coefficient increases in one case and decreases in the other. But as the increase in the case of monthly data may be traced back to the higher smoothing parameter, we feel legitimized to emphasize the explanation that the output gap reduces as soon as real time data are used.

5.3 Estimations of Taylor rules based on real time data – current period forecasts and „true” forecasts versus original real time data

So far we compared the relative performance of Taylor rule estimations dependent on the use of ex-post data or of real time data, the data set available to the ECB at the time it has to make their decision. In the following, we check whether our estimations based on real time data change if we implement real time forecasts. If we find significant numerical estimation differences between both types of Taylor rules we are able to distinguish the effects that the use of real time data has from the ones that are essentially induced by the application of a forecast based on real time data.

By this, we clearly go beyond those comparative studies which consider those two effects simultaneously and, hence, risk to mix both effects up (as, e.g., Gorter, Jacobs and De Haan (2008)). We would like to argue that the latter are unable to identify whether both effects played a role or (even more important) whether the results are driven by only one source with the other having no influence. In order to clarify issues in that respect, we display our Taylor rule estimations based on forecasted macro variables without interest rate smoothing and two different forecasts in Table 3.
Using the forecast for the current period (which becomes necessary as monetary policy operates with a lag) delivers almost the same results as the real time data in Table 1 did (columns 3.1-3.6 and 1.7-1.12). In fact, it even strengthens the pattern detected by increasing the inflation parameter even more and by simultaneously decreasing the output response. However, it has to be mentioned that by introducing these forecast the adjusted $R^2$ drops sharply for quarterly data (columns 3.4-3.6).

If we use “true” forecasts columns (3.7-3.12), with a horizon of six months for inflation and of three months for the output gap, the overall picture changes dramatically. As displayed in Table 3, columns 3.7 to 3.9, in two of the three monthly specifications (columns 3.7 and 3.9) the Taylor rule explains virtually nothing since all coefficients are insignificant. In the remaining specification (3.8), the estimated coefficients turn out to be significant but the Taylor principle is clearly violated while the output gap parameter stays more or less unchanged.

For quarterly data, the goodness-of-fit of the regression equation is rather low as measured by the adjusted $R$-squared. A closer inspection of the results in columns 3.10 to 3.12 reveals that the importance of the output gap is going to rise when forecasts based on real time data are used as input variables. In all three specifications the estimated output gap coefficients are larger than their real time counterparts which were displayed in columns 1.10 to 1.12 in Table 1. However, the inflation parameter in the “truly” forecasted Taylor rules in most cases turns out to take values far below unity (columns 3.11 and 3.12). But when applying the HP-Filter as a measure of potential output the inflation parameter is even increasing.\(^{16}\)

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\(^{16}\)The impression also conveyed by the results depicted in Table 4 is that the use of quarterly HP estimates has the potential to alter the estimation results significantly.
Nevertheless, it is by no means granted that results generated with the help of the HP-Filter are superior to others.

5.4 Estimations of Taylor rules with interest rate smoothing based on real time data – current period forecasts and „true“ forecasts versus original real time variables

In the final part of our comparative investigation exercise, we check for the relative performances of Taylor reaction functions based on time series of macro variables generated by current period forecasts and “true” forecasts. Our estimation results are shown in Table 4.

- Table 4 about here -

The high degree of interest rate smoothing at a monthly frequency (columns 4.1 to 4.3 and 4.7 to 4.9) already identified by us in section 5.2 can also be supported by the forecasts even though the smoothing parameters on average turn out to be slightly lower here compared to our estimates which used real time data (columns 2.7 to 2.9), in turn leading to more significant inflation and output gap coefficients. With respect to the inflation coefficient our result from section 5.3 that reactions are even stronger when current forecasts are used is reinforced while for truly forward looking Taylor rules this is not the case as it was also found in section 5.3.\(^{17}\) However, the estimated output gap coefficient amounts to 0.54 for current forecasts (column 4.2) and 0.26 (column 4.8) for truly forward looking forecasts and, hence, remains quite close to its real time counterpart (0.37 in column 2.8).

\(^{17}\) However this comparison has to rely on our estimates using the linear de-trended output gap because these were the only significant Taylor rule estimates when applying interest rate smoothing in real time.
If quarterly instead of monthly data are used (columns 4.4 to 4.6 and 4.10 to 4.12), the empirical pattern looks a bit different. Again, in the same way as for quarterly data in Table 2, the smoothing parameter differs quite considerably over the specifications, independent on what kind of forecast is applied. Moreover, for both types of forecasting the importance of the output gap parameter increases slightly and remains highly significant (row 4, columns 4.5 to 4.6 and 4.11 to 4.12, respectively) while the inflation coefficient decreases sharply taking even values lower than unity thus violating the Taylor principle (columns 4.5 to 4.6 and 4.11 to 4.12, respectively). 18 In fact, all but one (column 4.4) coefficients of the inflation rate become insignificant and in one case the sign of the estimated coefficients gets even negative (column 4.6).

Seen on the whole, thus, the following empirical picture emerges based on our partial results summarized in Tables 1 to 4 (sections 5.1 to 5.4). When estimating Taylor rules for the euro area with ex-post data, the estimated coefficient of inflation tends to be biased downwards and, in contrast, the estimated output gap coefficient turns out to be biased upwards (section 5.1) when compared to estimates using real time data. When we add an interest rate smoothing term to our empirical Taylor rule specification, the results are mainly reinforced. In this case, the estimations with the help of a linear de-trended output gap seem to perform best since they generate significant estimates of the Taylor rule coefficients.

When it comes to the implementation of forward looking elements into the Taylor rules using real time data (sections 5.3 and 5.4) the results are mainly reinforced at least as far as forecasts for the current period are concerned. In this

18 For quarterly data, we compare only the results of the Taylor rules using a linear and a quadratic de-trended output gap because in real time the results generated by the output gap with the HP-Filter delivered insignificant inflation and output gap coefficients due to the high interest smoothing parameter. Therefore, a comparison between this real time estimate and the forecasts is not possible.
case, the use of forecasts even strengthens the already identified differences between ex-post and real time data, i.e. that the inflation coefficient is rising while the output gap coefficient is falling slightly. Thus, when using “current period” forecasts the two effects of using real time instead of ex-post data and forecasts in real time rather than actual real time data tend to move in the same direction, meaning that both increase the response to inflation and lowering the output gap coefficient independently of each other.

However, when using “true” forecasts, our empirical results change. In this case, inflation turns out to be less important (in fact taking even values lower than unity thus violating the Taylor principle) while the output gap variable appears to be more in the focus of the ECB governing council. Hence, the effects of differences between ex-post and real time data and those induced by the use of real time forecasts instead of real time data tend to move in opposite directions. Here, the importance of dividing comparisons of ex-post data and forecasts using real time data into two separate steps becomes obvious as when applying a comparison between ex-post and real time data it turns out that inflation gets more important and output gap less important in real time while the use of forecasts lessens the importance of inflation and strengthens the response to the output gap.

6. Conclusions

In this paper we have shown that, in the case of the ECB, considerable differences of the estimated parameter values between Taylor rules emerge when ex post data are used instead of real-time data and vice versa. Accordingly, we are able to reproduce
a pattern of results which has quite frequently been identified in the literature for other central banks as well.\textsuperscript{19}

However, our empirical results reveal that in real time the inflation rate is of greater importance than it has been ex-post while the reverse is true for the output gap. Thus, our results do not give support to the results gained by Gerdesmeier and Roffia (2004) who found a stronger reaction to output and a weaker response to inflation in the real time data case. According to our analysis, these differences could be attributed to the different sample period and the different choice of instruments when estimating using GMM. However, our results are in line with those found by Sauer and Sturm (2007), but only if we employ the Taylor rule without interest rate smoothing.

When it comes to the discussion of using forecasted variables in Taylor rule estimation equations the overall evidence is mixed. However, when preparing its interest rate decisions, the ECB governing council is well known to react not only to currently available data but also to (medium-term) forecasts concerning future key variables as, above all, the inflation rate and the output gap. However, when using forecasts in Taylor rule estimations, the problem is that these forecasts need to be as close as possible to the unknown forecasts the ECB governing council actually bases its decision on. As full coincidence can never be guaranteed, using forecasts always tends to introduce an additional but unavoidable source of differences of estimation results which is not at all related to the difference between ex-post and real time data.

In our analysis, we separated the two effects - the first induced by the use of ex-post instead of real time data and the second caused by the use of forecasts based on real time data instead of the original real time data - to show whether the use of

forecasts promotes or distorts the results given by a mere comparison between ex-post and real time data. We found that any sound judgment on this question depends crucially on the choice of the forecast horizon. While in the case of forecasts for the current period the effects get even strengthened as expressed by even higher inflation and lower output responses, the reverse is true when really forward looking (“true”) forecasts are implemented. That is why we feel legitimized to recommend comparing Taylor rule coefficients with ex-post data and forecasts based on real time data within the three-step approach used here in order to single out the driver of the differences between these two estimates.
Figures

**Figure 1:** Real equilibrium interest rates. Source: EABCN and own calculations. The blue lines (E_R_IR_EXPOST) show the equilibrium real interest rate calculated with ex-post data while the red line (E_R_IR_RT) covers the same variable if real time data are used.

**Figure 2:** Inflation rates ex-post and in real time, source: EABCN and own calculations. The blue line (INFL_EXPOST) shows the inflation rate calculated with ex-post data and the red line (INFL_RT) covers the inflation rate variable available to policy decision makers in real time.
Figure 3: Output gaps ex-post and in real time. Source: EABCN and own calculations. The blue lines cover the output gaps estimated using ex-post data while the red lines show those if real time data are used, the abbreviations HP, LIN, QUA signal that potential output for this output gap is estimated using the HP-Filter, linear trend or quadratic trend.
### Tables

#### Table 1: Original Taylor rule estimates (eq. 2a);

<table>
<thead>
<tr>
<th>Ex-post data</th>
<th>Real time data</th>
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<tbody>
<tr>
<td>(1.1)</td>
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<tr>
<td>$Y_{M_H}$</td>
<td>$Y_{M_L}$</td>
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<tr>
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<tr>
<td>J-stat</td>
<td>0.06</td>
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Notes: GMM estimates, */ **/ *** denote significance at the 10%/ 5%/ 1% level, standard errors in parenthesis, for J-statistic p-value in parenthesis; M=monthly estimate, Q=quarterly estimate, HP=HP-Filter, LIN=linear trend, QUA=quadratic trend used.

#### Table 2: Taylor rule estimates with interest rate smoothing (eq. 3a);

<table>
<thead>
<tr>
<th>Ex-post data</th>
<th>Real time data</th>
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<tbody>
<tr>
<td>(2.1)</td>
<td>(2.2)</td>
</tr>
<tr>
<td>$Y_{M_H}$</td>
<td>$Y_{M_L}$</td>
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<tr>
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<tr>
<td>$a_\pi$</td>
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<tr>
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</table>

Notes: GMM estimates, */ **/ *** denote significance at the 10%/ 5%/ 1% level, standard errors in parenthesis, for J-statistic p-value in parenthesis; M=monthly estimate, Q=quarterly estimate, HP=HP-Filter, LIN=linear trend, QUA=quadratic trend used.

#### Table 3: Taylor rule estimates based on forecast macro variables – Real time data (eq. 4a);

<table>
<thead>
<tr>
<th>Forecast for current period</th>
<th>Forecast inflation 6M / output gap 3M</th>
</tr>
</thead>
<tbody>
<tr>
<td>(3.1)</td>
<td>(3.2)</td>
</tr>
<tr>
<td>$Y_{M_H}$</td>
<td>$Y_{M_L}$</td>
</tr>
<tr>
<td>$a_0$</td>
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</tr>
<tr>
<td>$a_\pi$</td>
<td>0.08</td>
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<td>$a_y$</td>
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<tr>
<td>$adj R^2$</td>
<td>0.12</td>
</tr>
<tr>
<td>J-stat</td>
<td>0.06</td>
</tr>
</tbody>
</table>

Notes: GMM estimates, */ **/ *** denote significance at the 10%/ 5%/ 1% level, standard errors in parenthesis, for J-statistic p-value in parenthesis; M=monthly estimate, Q=quarterly estimate, HP=HP-Filter, LIN=linear trend, QUA=quadratic trend used.
<table>
<thead>
<tr>
<th>Forecast for current period</th>
<th>Forecast inflation 6M / output gap 3M</th>
</tr>
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<tbody>
<tr>
<td>( y_M^{MP} )</td>
<td>( y_M^{LN} )</td>
</tr>
<tr>
<td>( y_M^{Q4A} )</td>
<td>( y_M^{Q1A} )</td>
</tr>
<tr>
<td>( y_Y^{MP} )</td>
<td>( y_Y^{LN} )</td>
</tr>
<tr>
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<tr>
<td>( a_\pi )</td>
<td>( a_Y )</td>
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<tr>
<td>( adj \ R^2 )</td>
<td>( J\text{-stat} )</td>
</tr>
<tr>
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<td>(4.11)</td>
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<td>(4.12)</td>
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</table>

Table 4: Taylor rule estimates with interest rate smoothing based on forecasted variables (eqs. (3a) and 4a)); Notes: GMM estimates, \(*/ /**/ ***\) denote significance at the 10%/ 5%/ 1% level, standard errors in parenthesis, for J-statistic p-value in parenthesis; M=monthly estimate, Q=quarterly estimate, HP=HP-Filter, LIN=linear trend, QUA=quadratic trend used.
References


